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**ON THE SMOOTHNESS OF WEAK SOLUTIONS OF
STRONG-NONLINEAR NONDIAGONAL ELLIPTIC
SYSTEMS (THE TWO-DIMENSIONAL CASE)**

ABSTRACT. We consider a class of strong-nonlinear elliptic systems with a nondiagonal principal matrix. Weak solvability of the Dirichlet problem for such type systems was earlier proved by the author in the two-dimensional case. The solution constructed was smooth almost everywhere. Here we prove that this solution is a Hölder continuous function in the entire domain.

**Dedicated to the memory of
Olga Aleksandrovna Ladyzhenskaya**

In [1], the author proved the existence of a weak solution for the following Dirichlet problem:

$$\left. \begin{aligned} \frac{d}{dx_\alpha} a_\alpha^k(x, u, u_x) + b^k(x, u, u_x) &= 0, \quad k = 1, \dots, N, \quad x \in \Omega, \\ u|_{\partial\Omega} &= 0, \end{aligned} \right\} \quad (1)$$

where Ω is a bounded domain in \mathbb{R}^2 with smooth boundary $\partial\Omega$; $u : \Omega \rightarrow \mathbb{R}^N$, $N > 1$, $u = (u^1, \dots, u^N)$, $u_x = \{u_{x_\alpha}^k\}_{\alpha \leq 2}^{k \leq N}$.

It was assumed in [1] that the functions $a_\alpha = \{a_\alpha^k\}_{k \leq N}$, $\alpha = 1, 2$, and $b = \{b^k\}_{k \leq N}$ are differentiable on the set $\mathfrak{M} = \overline{\Omega} \times \mathbb{R}^N \times \mathbb{R}^{2N}$ and

$$|a_\alpha(x, u, z)| \leq \mu_1(1 + |z|), \quad |b_\alpha(x, u, z)| \leq \mu_2(1 + |z|^2), \quad (2)$$

Moreover, we postulated also the natural behavior of all the derivatives and the ellipticity condition in the strong form

$$\frac{\partial a_\alpha^k(x, u, z)}{\partial z_\beta^l} \xi_\alpha^k \xi_\beta^l \geq \nu |\xi|^2, \quad \xi \in \mathbb{R}^{2N}; \quad \left\| \frac{\partial a}{\partial z}(x, u, z) \right\| \leq \mu_1. \quad (3)$$

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Here, the constants μ_1 , μ_2 , and ν are fixed arbitrarily.

The second condition in (2) describes the quadratic (limit) growth in the gradient of the function b .

The existence of a weak solution $u \in \overset{\circ}{W}_2^1(\Omega)$ of (1) (in the sense of distributions) was proved in [1] under the additional condition

$$a_\alpha(x, u, z)z_\alpha + b(x, u, z)u \geq \nu_0|z|^2 - \mu_0, \quad (x, u, z) \in \mathfrak{M}, \quad (4)$$

where $\nu_0, \mu_0 = \text{const} > 0$.

The solution u is $C^{2+\alpha}$ -smooth almost everywhere in $\overline{\Omega}$ with $\alpha \in (0, 1)$, and the singular set σ consists of at most finitely many points (see [1, Theorem 1 and Remark 1]). This solvability result is a simple consequence of the theorem on the *quasireverse* Hölder inequalities proved by the author in [2].

Analyzing the proof of Theorem 1 in [1], one can deduce the existence of a weak solution of (1) in the class $\overset{\circ}{W}_2^1(\Omega) \cap C^\alpha(\overline{\Omega} \setminus \sigma)$ under less restrictive assumptions on the data than (3). More precisely, it is enough to require that condition (2), (4) and the inequality

$$(a_\alpha(x, u, z) - a_\alpha(x, u, \zeta))(z_\alpha - \zeta_\alpha) \geq 0, \quad (x, u) \in \overline{\Omega} \times \mathbb{R}^N, \quad z, \zeta \in \mathbb{R}^{2N}, \quad (5)$$

hold. In this case, we do not assume the existence of the derivatives of a_α and b .

Conditions (2), (4), and (5) are close to assumptions in [3], where J. Freshe proved the existence of a solution of problem (1) in the class $\overset{\circ}{W}_2^1(\Omega) \cap C^\alpha(\overline{\Omega})$, $\alpha \in (0, 1)$.

Note that the coerciveness condition was required in [3] in a slightly stronger form than in (4).

Remark 1. We can allow the functions a_α and b to have a power growth in the argument “ u ,” as it was done in [3]. This is not essential if the coerciveness property of the operator is preserved.

Remark 2. It is easy to see that the conditions $a_\alpha(x, u, z)z_\alpha \geq \nu|z|^2 - \mu_3$ and the so-called “one-sided condition” $b(x, u, z)u \geq -\nu_*|z|^2 - \mu_3, \nu - \nu_* > 0$, provide the validity of assumption (4).

Paper [1] had already been published when the author proved that a weak solution constructed in [1] under conditions (2), (4), and (5) is a Hölder function in the entire domain $\overline{\Omega}$, i.e., $\sigma = \emptyset$. The aim of this note to explain this fact.

The method of approximations in [1] and in the present paper seriously differs from that in [3]. At the same time, we essentially use J. Freshe's idea of the estimation of local energy norms of approximations with the help of the inequality

$$\frac{1}{r^2} \int_{\Omega_r(x^0)} |v|^2 dx \leq K |\ln r| \|v\|_{W_2^1(\Omega)}^2 \quad \text{for } v \in \mathring{W}_2^1(\Omega), \quad n = 2, \quad (6)$$

$\Omega_r(x^0) = \Omega \cap B_r(x^0)$, $x^0 \in \overline{\Omega}$, $r \leq \frac{1}{2}$, $K = K(\Omega) = \text{const} > 0$ (see [3, Lemma 2.4]).

In this note, we accept all the notation from [1] and prove the following result.

Theorem. *Let Ω be a bounded domain in \mathbb{R}^n with Lipschitz boundary $\partial\Omega$. Let the functions $a_\alpha(x, u, z)$ and $b(x, u, z)$ be defined on $\mathfrak{M} = \overline{\Omega} \times \mathbb{R}^N \times \mathbb{R}^{2N}$ and let them be measurable in x and continuous in (u, z) on \mathfrak{M} .*

Let conditions (2), (4), and (5) hold. Then a solution $u \in \mathring{W}_2^1(\Omega) \cap C^\alpha(\overline{\Omega})$ of problem (1) with a certain $\alpha \in (0, 1)$ exists.

To prove the theorem, we consider the same approximations of (1) as in [1]:

$$\left. \begin{aligned} -\frac{d}{dx_\alpha} \left(a_\alpha^k(x, u, u_x) + \varepsilon u_{x_\alpha}^k (1 + |u_x|^2)^{\frac{m}{2}-1} \right) + b^k(x, u, u_x) &= 0, \\ k = 1, \dots, N, \quad x \in \Omega; \quad u|_{\partial\Omega} &= 0, \quad \varepsilon \in (0, 1]. \end{aligned} \right\} \quad (7)$$

We shall choose the parameter $m > 2$ below.

By the Leray–Lions theory, conditions (2), (4), and (5) guarantee the existence of a solution $u^\varepsilon \in \mathring{W}_m^1(\Omega)$ of (7) for any fixed $\varepsilon \in (0, 1]$.

By the embedding theorem, $u^\varepsilon \in C^\beta(\overline{\Omega})$, where $\beta = 1 - \frac{2}{m} > 0$. From condition (2), it follows that

$$\|u_x^\varepsilon\|_{L_2(\Omega)}^2 + \varepsilon \|u_x^\varepsilon\|_{L_m(\Omega)}^m \leq \mathbf{e}_0, \quad (8)$$

where the constant \mathbf{e}_0 depends on the parameters ν_0 , μ_0 , and $|\Omega|$, but not on $\varepsilon \in (0, 1]$. It follows from (8) that for a sequence $\{\overline{\varepsilon}\} \rightarrow 0$, $u_{x^\varepsilon}^\varepsilon \rightarrow u_x$ in $L_2(\Omega)$, $u^\varepsilon \rightarrow u$ almost everywhere in Ω , $\overline{\varepsilon}^{\frac{1}{m}} u_x^\varepsilon \rightarrow 0$ in $L_m(\Omega)$, $u \in \mathring{W}_2^1(\Omega)$. We shall prove that the function u is a solution of problem (1) Hölder continuous in $\overline{\Omega}$.

The following fact was proved in [1, Proposition 2]:

“There exist numbers $\theta_0 > 0$ and $p > 2$, dependent only on the parameters from (2) and (4), such that the inequality

$$\int_{\Omega_0(x^0)} \left[|u_x^{\varepsilon_i}|^2 + \varepsilon_i \left(|u_x^{\varepsilon_i}|^2 + 1 \right)^{\frac{m}{2}} \right] dx < \theta_0^2 \quad (9)$$

provides the estimate

$$\|u_x^{\varepsilon_i}\|_{L_p(\Omega_{\frac{R_0}{2}}(x^0))} \leq c_1, \quad (10)$$

where the constant c_1 does not depend on $\{\varepsilon_i\}$, and $\{\varepsilon_i\}$ is a subsequence of the sequence $\{\bar{\varepsilon}\}$.”

Remark 3. The constant c_1 in (10) and the constants c and c_i in the paper may depend on the parameters $\nu_0, \mu_0, \mu_1, \mu_2$, and $|\Omega|$, but not on ε . In what follows, we write ε instead of $\bar{\varepsilon}$.

We note that estimate (10) implies the estimate

$$\|u^{\varepsilon_i}\|_{C^\alpha(\Omega_{\frac{R_0}{2}}(x^0))} \leq c_2, \quad \alpha = 1 - \frac{2}{p} > 0. \quad (11)$$

It follows from (11) that the limit function u is Hölder continuous in the vicinity of the point x^0 . In this paper, we prove that for the whole sequence $\varepsilon \rightarrow 0$ and for all point $x^0 \in \bar{\Omega}$, we have the estimate

$$\int_{\Omega_R(x^0)} \left(|u_x^\varepsilon|^2 + \varepsilon \left(1 + |u_x^\varepsilon|^2 \right)^{\frac{m}{2}} \right) dx \leq \tau(R) \quad (12)$$

with a certain function $\tau(R)$, where $\tau(R) \rightarrow 0$ as $R \rightarrow 0$, and $\tau(R)$ does not depend on x^0 and ε .

Obviously, inequality (12) ensures the validity of condition (9) and the theorem.

First we note that the following global estimate holds for u^ε :

$$\int_{\Omega} |u^\varepsilon|^\gamma |u_x^\varepsilon|^2 dx \leq \mathbf{e}_1, \quad \gamma \in \left(0, \frac{2\nu_0}{3\mu_1} \right), \quad (13)$$

and the constant \mathbf{e}_1 does not depend on $\varepsilon \in (0, 1]$.

Indeed, the function u^ε satisfies the identity

$$\int_{\Omega} \left[a_\alpha(x, u^\varepsilon, u_x^\varepsilon) h_{x_\alpha} + \varepsilon u_{x_\alpha}^\varepsilon (1 + |u_x^\varepsilon|^2)^{\frac{m}{2}-1} h_{x_\alpha} + b(x, u^\varepsilon, u_x^\varepsilon) h \right] dx = 0, \quad \forall h \in \overset{\circ}{W}_m^1(\Omega). \quad (14)$$

From (14) with $h = u^\varepsilon |u^\varepsilon|^\gamma$ and $\gamma \in \left(0, \frac{2}{3} \frac{\nu_0}{\mu_1}\right)$, we derive the inequality

$$\left(\nu_0 - \frac{3}{2}\gamma\mu_1\right) \int_{\Omega} |u_x^\varepsilon|^2 |u^\varepsilon|^\gamma dx \leq c(\gamma, \mu_0, \mu_1) \int_{\Omega} (|u^\varepsilon|^2 + 1) dx.$$

Together with (8), it yields estimate (13).

To derive (12), we define the function G by the relation

$$G^2(x) = 1 + \nu_0 |u_x^\varepsilon(x)|^2 + \varepsilon |u_x^\varepsilon(x)|^m, \quad x \in \overline{\Omega}, \quad (15)$$

and henceforth we fix the number m by the relation

$$m = 2 + \gamma, \quad (16)$$

where γ is the parameter from (13).

Following the proof of Lemma 2.5 in [3], we fix a number $\omega > 0$ and sequences of radii $R_j = \frac{1}{2^j}$ and numbers θ_j satisfying the relation

$$(1 + \theta_j)^{-1} = \left(1 - \frac{1}{j}\right)^\omega, \quad j \in \mathfrak{N}. \quad (17)$$

For a fixed j , we put $R = R_j$, $2R = R_{j-1}$, and $\theta = \theta_j$ and prove the following proposition.

Proposition. *The function G satisfies the inequality*

$$\int_{\Omega_R(x^0)} G^2 dx \leq \frac{1}{1+\theta} \int_{\Omega_{2R}(x^0)} G^2 dx + C_3 J(R, \theta), \quad (18)$$

where $x^0 \in \partial\Omega$ or $x^0 \in \Omega$ and $2R \leq \text{dist}\{x^0, \partial\Omega\}$. Here $J(R, \theta) = \theta^2 |\ln R|^{\frac{2}{m}} + R^2 + \theta^{\frac{m}{2}+1} |\ln R|$ if $\varepsilon \leq \left(\frac{R}{\sqrt{\theta}}\right)^{m-2}$, and $J(R, \theta) = R^2$ if $\varepsilon > \left(\frac{R}{\sqrt{\theta}}\right)^{m-2}$ and $\theta \leq \theta_*$ for a number θ_* dependent only on the data.

Proof of the proposition. First, let $\varepsilon \leq \left(\frac{R}{\sqrt{\theta}}\right)^{m-2}$ and $x^0 \in \overline{\Omega}$ be fixed arbitrarily. From (14) with $h = u^\varepsilon \zeta^2$, where ζ is a cut-off function for the ball $B_{2R}(x^0)$, $\zeta = 1$ in $B_R(x^0)$, we obtain

$$\begin{aligned} \int_{\Omega_{2R}} G^2 \zeta^2 dx &\leq 2\varepsilon \int_{\Omega_{2R}} |u_x| (1 + |u_x|^2)^{\frac{m}{2}-1} |u| \zeta |\zeta_x| dx + \\ &+ \int_{\Omega_{2R}} |a_\alpha| |u| 2\zeta |\zeta_x| dx + (\mu_0 + 1)\pi R^2 \equiv j_1 + j_2 + j_3. \end{aligned} \quad (19)$$

In (19) and below, we write u and Ω_r instead of u^ε and $\Omega_r(x^0)$, respectively.

We denote $T_{2R} = \Omega_{2R} \setminus \Omega_R$ and estimate the integrals j_1 and j_2 in (19).

By the Cauchy inequality, we find that

$$\left. \begin{aligned} j_1 &\leq \frac{\varepsilon}{\theta} \int_{T_{2R}} |u_x|^m dx + \frac{c(m)\varepsilon}{R^m} \theta^{m-1} \int_{T_{2R}} |u|^m dx + \frac{c\varepsilon}{R} \int_{T_{2R}} |u| dx; \\ j_2 &\leq \frac{\nu_0}{\theta} \int_{T_{2R}} |u_x|^2 dx + c(\nu_0, \mu_1) \frac{\theta}{R^2} \int_{T_{2R}} |u|^2 dx. \end{aligned} \right\} \quad (20)$$

Now, we put $v = |u^\varepsilon|^{\frac{m}{2}}$ in (6) to assert that

$$\left. \begin{aligned} \frac{1}{R^2} \int_{\Omega_{2R}(x^0)} |u^\varepsilon|^m dx &\leq c |\ln R| \int_{\Omega} (|u^\varepsilon|^m + |u^\varepsilon|^{m-2} |u_x^\varepsilon|^2) dx \leq \\ &\stackrel{(8),(13)}{\leq} c_4 |\ln R|. \end{aligned} \right\} \quad (21)$$

By the Hölder inequality, from (21) we have

$$\begin{aligned} \frac{1}{R^2} \int_{\Omega_{2R}(x^0)} |u^\varepsilon|^2 dx &\leq c_5 |\ln R|^{\frac{2}{m}}; \\ \frac{\varepsilon}{R} \int_{\Omega_{2R}(x^0)} |u^\varepsilon| dx &\leq c_6 \varepsilon R |\ln R|^{\frac{1}{m}}. \end{aligned} \quad (22)$$

From (19), (20), (21), and (22), we deduce the inequality

$$\left. \begin{aligned} \int_{\Omega_R} G^2 dx &\leq \frac{1}{\theta} \int_{T_{2R}} G^2 dx + \\ &+ c_7 \left(\frac{\varepsilon \theta^{m-1}}{R^{m-2}} |\ln R| + \theta |\ln R|^{\frac{2}{m}} + \varepsilon R |\ln R|^{\frac{1}{m}} + R^2 \right). \end{aligned} \right\} \quad (23)$$

By the standard ‘‘hole-filling’’ technique, from (23) we obtain estimate (18) under restriction $\varepsilon \leq \left(\frac{R}{\sqrt{\theta}}\right)^{m-2}$.

Let now $\varepsilon > \left(\frac{R}{\sqrt{\theta}}\right)^{m-2}$ and $x^0 \in \partial\Omega$ or $x^0 \in \Omega$ and $2R \leq \text{dist}(x^0, \partial\Omega)$.

In this case, we put $h = (u - l_R)\zeta^m$, where $l_R = 0$ if $x^0 \in \partial\Omega$, and $l_R = \int_{T_{2R}} u dx$ if $x^0 \in \Omega$ and $2R \leq \text{dist}(x^0, \partial\Omega)$; ζ is the same cut function as before. In both cases, the function h is admissible for identity (14), and the following inequality is valid:

$$\begin{aligned} &\int_{\Omega_{2R}} \left(a_\alpha u_{x_\alpha} + \varepsilon |u_x|^2 (1 + |u_x|^2) \right)^{\frac{m-2}{2}} \zeta^m dx \leq \\ &\leq m\mu_1 \int_{T_{2R}} (1 + |u_x|) |u - l_R| \zeta^{m-1} |\zeta_x| dx + \int_{\omega_{2R}} |b| |u - l_R| \zeta^m dx + \\ &+ \varepsilon c(m) \int_{T_{2R}} (1 + |u_x|^{m-1}) \zeta^{m-1} |u - l_R| |\zeta_x| dx. \end{aligned} \quad (24)$$

We estimate the integral with the function $|b|$ in (24) in the way

$$\begin{aligned} \mathcal{L}_R &= \int_{\Omega_{2R}} |u_x|^2 |u - l_R| \zeta^m dx \leq \\ &\leq \left(\int_{\Omega_{2R}} |u_x|^m \zeta^m dx \right)^{\frac{2}{m}} \left(\int_{\Omega_{2R}} |u - l_R|^{\frac{m}{m-2}} dx \right)^{\frac{m-2}{m}} \leq \\ &\stackrel{(*)}{\leq} c \left(\frac{\varepsilon}{4} \int_{\Omega_{2R}} |u_x|^m \zeta^m dx \right)^{\frac{2}{m}} \left(\int_{\Omega_{2R}} |u_x|^2 dx \right)^{\frac{1}{2}} \frac{R^{2(1-\frac{2}{m})}}{\varepsilon^{\frac{2}{m}}} \leq \end{aligned}$$

$$\begin{aligned}
& \stackrel{(**)}{\leq} c\theta^{\frac{m-2}{m}} \left(\frac{\varepsilon}{4} \int_{\Omega_{2R}} |u_x|^m \zeta^m dx \right)^{\frac{2}{m}} \left(\int_{\Omega_{2R}} |u_x|^2 dx \right)^{\frac{1}{2}} \leq \\
& \leq \frac{\varepsilon}{4} \int_{\Omega_{2R}} |u_x|^m \zeta^m dx + c\theta e_0^{\frac{4-m}{2(m-2)}} \int_{\Omega_{2R}} |u_x|^2 dx.
\end{aligned}$$

Here the inequality (*) is valid by the embedding theorem $W_2^1(\Omega_{2R}) \hookrightarrow L_{\frac{m}{m-2}}(\Omega_{2R})$, $n = 2$, and the inequality (**) holds, because $\varepsilon > \left(\frac{R}{\sqrt{\theta}}\right)^{m-2}$.

Now, from (24) it follows that

$$\int_{\Omega_R} G^2 dx \leq c_8 \int_{T_{2R}} G^2 dx + c_9 \theta \int_{\Omega_{2R}} G^2 dx + c_{10} R^2. \quad (25)$$

Now we fix a number θ satisfying the restriction

$$\theta \leq \theta_* = \min \left\{ \frac{1}{2c_9}; \frac{1}{2c_8 + 1} \right\}, \quad (26)$$

and note that in this case

$$\frac{c_8 + \frac{1}{2}}{c_8 + 1} \leq \frac{1}{1 + \theta}.$$

By the ‘‘hole-filling’’ technique, we derive (18) from (25) under condition (26) and the restriction $\varepsilon > \left(\frac{R}{\sqrt{\theta}}\right)^{m-2}$. The proposition is proved. \square

Proof of the theorem. Let the location of a point $x^0 \in \overline{\Omega}$ be the same as it is indicated in the proposition. Recalling the notation of R and θ , we note that definition (17) yields the estimate $\theta = \theta_j \leq \frac{2\omega}{j}$ for $j \geq 2$. Moreover, we consider

$$j \geq j_0 = \max \left\{ 2, \frac{2\omega}{\theta_*} \right\}$$

to satisfy the restriction $\theta_j \leq \theta_*$ (θ_* is fixed in the proposition).

From (18) and (17), we obtain the inequality

$$\begin{aligned}
& \int_{\Omega_{R_j}} G^2 dx \leq \\
& \leq \left(\frac{j-1}{j}\right)^\omega \int_{\Omega_{R_{j-1}}} G^2 dx + c_3 \left(\theta_j^2 |\ln R_j|^{\frac{2}{m}} + R_j^2 + \theta_j^{\frac{m}{2}+1} |\ln R_j| \right) \quad (27)
\end{aligned}$$

under any relation between ε and $\left(\frac{R_j}{\sqrt{\theta_j}}\right)^{m-2}$.

Since $|\ln R_j| = j \ln 2$, we have

$$j^\omega \int_{\Omega_{R_j}} G^2 dx \leq (j-1)^\omega \int_{\Omega_{R_{j-1}}} G^2 dx + c_{11} \left(j^{\omega + \frac{2}{m} - 2} + j^{\omega + 1 - \frac{m}{2} - 1} + \frac{j^\omega}{4^j} \right).$$

From the last inequality, it follows that

$$\begin{aligned} j^\omega \int_{\Omega_{R_j}} G^2 dx &\leq \\ &\leq (j_0 - 1)^\omega \int_{\Omega_{R_{j_0-1}}} G^2 dx + c_{12} \sum_{i=j_0}^j \left(\frac{j^\omega}{4^i} + \frac{1}{i^{2-\omega-\frac{2}{m}}} + \frac{1}{i^{\frac{m}{2}-\omega}} \right). \end{aligned} \quad (28)$$

Now fix $\omega \in \left(0, \frac{m-2}{m}\right)$ to ensure the convergence of the series and (28) derive the estimate

$$\int_{\Omega_{R_j(x_0)}} G^2 dx \leq \frac{c_{13}}{|\ln R_j|^\omega}. \quad (29)$$

It is easy to see that the estimate

$$\int_{\Omega_{R_j(x_0)}} G^2 dx \leq \frac{c_{13}}{|\ln 2R_j|^\omega}, \quad j \geq j_0 + 1$$

is valid for an arbitrary location of x^0 in $\overline{\Omega}$. Obviously, this implies estimate (12). The theorem is proved. \square

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